

Problem Solving

Employees in 2012 paid 4.2% of their gross wages towards social security (FICA tax),

How much will someone earning \$74,000 a year pay towards social security out of their gross wages?

Problem Solving

= 4.2% of \$74,000

$$= 4.2\% = \frac{4.2}{100} = 0.042$$

= 0.0042 of \$74,000

$$= 0.0042 * \$74,000$$

= \$3,108

Absolute & Relative Changes

The population of a town increased from 3500 in 2005 to 5450 in 2012.

Find the absolute and relative (percent) increase.

Absolute & Relative Changes

Increased from 3500 to 5450

Absolute Increase

= Actual Change from 3500 to 5450

= 1950

Relative (percent) increase *(from original)*

$$= (1950 / 3500) = 0.5571$$

≈ 55.7 %

Multiple % Discounts

A store has clearance items that have been marked down by 20%. They are having a sale, advertising an additional 60% off clearance items. What percent of the original price do you end up paying?

Multiple % Discounts

Original marked down by 20%
With additional 60% off

Example:

Original Price is \$100
 $\$100 * 0.20 = \20 off
 Sale Price is $\$100 - \$20 = \$80$
 Additional 60% off so $\$80 * 0.60 = \48 off
 Final Price is $\$80 - \$48 = \$32$

Multiple % Discounts

Original marked down by 20%
You pay 80%

With additional 60% off
You pay 40%

Example:

Original Price is \$100
 $\$100 * 0.80 * 0.40 = \$100 * 0.32 = \$32$

Multiple Percent Discounts

A store has clearance items that have been marked down by 20%. They are having a sale, advertising an additional 60% off clearance items. What percent of the original price do you end up paying?

Answer:

$$= (100\% - 20\%) * (100\% - 60\%)$$

$$= 0.8 * 0.4 = 0.32$$

$$= 32\%$$

Weighted Percent

Total = (Weight * Score) + (Weight * Score) + ...

- **Homework** : 40%
- **Class Preparation and Participation**: 10%
- **Quizzes**: 25%
- **Tests**: 16%
- **Final**: 9%

$$\text{Total} = (0.40 * \text{HW}) + (0.10 * \text{Class}) + (0.25 * \text{Quiz})$$

$$+ (0.16 * \text{Test}) + (0.09 * \text{Final})$$

Weighted Percent

You have a 83% average before the final exam. That score includes everything but the final, which counts for 25% of the course grade.

What are your worst and best possible grades?

Final is 25% so everything else is 75%
 Worst grade = $0.75 * 0.83 = 0.6225 = 62.25\%$
 Best grade = $0.6225 + 0.25 = 0.8725 = 87.25\%$
 Note: Grade = $(0.75 * 0.83) + (0.25 * \text{FinalExam})$

Weighted Percent

You have a 83% average before the final exam. Final counts for 25% of the course grade.

What is the final exam score needed for 80%?

$$\text{Grade} = (0.75 * 0.83) + (0.25 * \text{FinalExam})$$

$$0.80 = (0.75 * 0.83) + (0.25 * \text{FinalExam})$$

$$0.80 = (0.6225) + (0.25 * \text{FinalExam})$$

$$0.1775 = (0.25 * \text{FinalExam})$$

$$\text{FinalExam} = 0.1775 / 0.25 = 0.71 = 71\%$$

Units

A car is driving at 70 kilometers per hour.
How far, in meters, does it travel in 4 seconds?

$$\frac{70\cancel{km}}{1\cancel{hr}} * \frac{1000m}{1\cancel{km}} * \frac{1\cancel{hr}}{60\cancel{min}} * \frac{1min}{60sec}$$

$$\frac{70}{1} * \frac{1000m}{1} * \frac{1}{60} * \frac{1}{60sec} = \frac{70000m}{3600sec}$$

$$\frac{700}{36} m/sec = \frac{175}{9} m/sec$$

Units

A car is driving at 70 kilometers per hour.
How far, in meters, does it travel in 4 seconds?

$$\frac{175}{9} m/sec$$

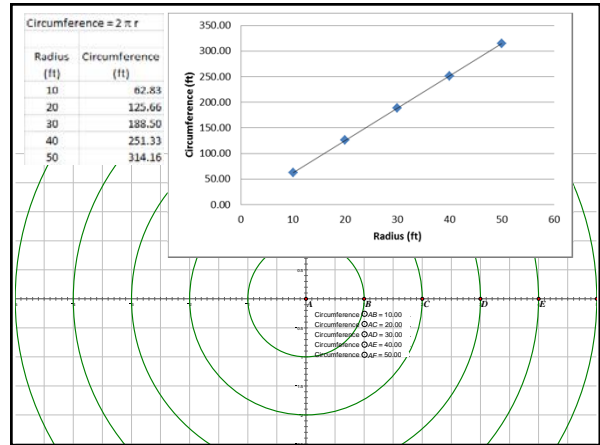
In 4 seconds:

$$\frac{175m}{9sec} * \frac{4sec}{1} = \frac{700m}{9} = 77.\bar{7}m$$

Answer: 78m

Exact vs Rounded Answers

One Third = 1/3
On Calculator: 0.33333333
or $0.\bar{3}$



Gears

(Shaft Speed₁)(# Teeth₁) = (Shaft Speed₂)(# Teeth₂)

$$S1 * T1 = S2 * T2$$

$$\frac{S1 * T1}{S2} = \frac{S2 * T2}{S2}$$

$$\frac{S1 * T1}{S2} = T2$$

Gears

(Shaft Speed₁)(# Teeth₁) = (Shaft Speed₂)(# Teeth₂)

Shaft		Axle	
S1	T1	S2	T2
Speed	# Teeth	# Teeth	Speed
100	300	= 300	100
100	300	= 150	200
100	300	= 100	300
100	300	= 75	400
100	300	= 60	500