



## Topics this Chapter

### Simple Interest

#### ▼ Simple Interest Formula

The simple interest formula is

$$I = Prt$$

### Compound Interest

#### ▼ Compound Amount Formula

The compound amount formula is

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

### Present Value

#### ▼ Present Value Formula

The present value formula is

$$P = \frac{A}{\left( 1 + \frac{r}{n} \right)^{nt}}$$

### Credit Cards

#### ▼ Average Daily Balance

Average daily balance =  $\frac{\text{sum of the total amounts owed each day of the month}}{\text{number of days in the billing period}}$

Consumer Loans: Calculating Monthly Payments

▼ **Payment Formula for an APR Loan**

The payment for a loan based on APR is given by

$$PMT = A \left( \frac{\frac{r}{n}}{1 - \left(1 + \frac{r}{n}\right)^{-nt}} \right)$$

Mortgages & Ongoing Expenses

▼ **Mortgage Payment Formula**

The mortgage payment for a mortgage is given by

$$PMT = A \left( \frac{\frac{r}{n}}{1 - \left(1 + \frac{r}{n}\right)^{-nt}} \right)$$

The screenshot shows the website daveramsey.com with a search bar and navigation tabs: Home, Get Started, The Show, Classes, Live Events, Tools, Dave Recommends, and Store. A 'Classes' dropdown menu is open, displaying various categories such as 'Financial Peace University', 'The Legacy Journey', 'Government/Military', 'Military', 'Government', 'For Business', 'Financial Wellness', 'Start a Workplace Class', 'For Kids and Teens', 'School Curriculum', 'Generation Change: Bible Study', 'Junior's Adventures (Ages 3-12)', 'For Bankruptcy Discharge', 'Debtor Education', 'Coaching', 'Financial Coaching', 'Nonprofits/Correctional', 'Nonprofits', 'Correctional Facilities', 'Spanish', and 'Andres Gutierrez'. A 'Dave & Rachel's New Book' banner is visible at the bottom.

The graphic features a portrait of Dave Ramsey on the left. To the right, the text reads 'DAVE RAMSEY'S SEVEN BABY STEPS'. Below this is the quote: 'Getting out of debt will not happen overnight; it takes time.' At the bottom, the logo for 'Dave Ramsey's Financial Peace UNIVERSITY' is displayed, along with the contact information '888.22.PEACE • daveramsey.com'.

step 1: \$1,000 In An Emergency Fund

step 2: Pay Off All Debt With The Debt Snowball

step 3: 3 To 6 Months Expenses In Savings

step 4: Invest 15% Of Income Into Roth IRAs And Pre-Tax Retirement Plans

step 5: College Funding

step 6: Pay Off Your Home Early

step 7: Build Wealth And Give!

Simple Interest:  $I = Prt$

- I = Interest earned.
- P = Principal:
- r = Annual % Rate:
- t = # of Years:

Principal:	500	800	2000	5000
Annual % Rate:	6.00	8.00	12.00	15.00
# of Years:	1	10	25	50
Simple Interest:	30	640	6000	37500
Total:	530	1440	8000	42500

Calculate simple interest due on a 3-month loan of \$2000 if the interest rate is 6.5%.

$$P = 2000 \qquad I = Prt$$

$$r = 6.5\% = 0.065$$

$$t = \frac{3 \text{ months}}{1 \text{ year}} = \frac{3 \text{ months}}{12 \text{ months}} = \frac{3}{12}$$

$$I = 2000(0.065)\left(\frac{3}{12}\right) = 32.5$$

Simple interest due is \$32.50.

## Simple Interest $t$

$$\text{Exact method: } t = \frac{\text{number of days}}{365}$$

$$\text{Ordinary method: } t = \frac{\text{number of days}}{360}$$

Average 30 days/month  $\cdot$  12 months = 360

The ordinary method is used by most businesses. Therefore, **unless otherwise stated, the ordinary method will be used.**

Calculate the simple interest due on a 45-day loan of \$3500 if the annual interest rate is 8%.

$$I = Prt$$

$$P = 3500, r = 8\% = 0.08, t = \frac{\text{number of days}}{360} = \frac{45}{360}$$

$$I = 3500(0.08)\left(\frac{45}{360}\right) = 35$$

The simple interest due is \$35.

## Future Value or Maturity Value Formula for Simple Interest

The future or maturity value formula for simple interest is

$$A = P + I$$

where  $A$  is the amount after the interest,  $I$ , has been added to the principal,  $P$ .

- So when you borrow money, the total amount to be repaid to the lender is the sum of the principal and interest.
- **Maturity Value:** For Loans  
 $A$  is the total amount to be repaid to the lender
- **Future Value:** For Investments  
 $A$  is the total amount on deposit after the interest earned has been added to the principal.

Calculate the maturity value of a simple interest, 8-month loan of \$8000 if the interest rate is 9.75%.

$$I = Prt$$

**Step 1:** Find the interest.

$$P = 8000, r = 9.75\% = 0.0975, t = \frac{8}{12}$$

$$I = 8000(0.0975)\left(\frac{8}{12}\right) = 520$$

**Step 2:** Find the maturity value.

$$A = P + I$$

$P = 8000$  and  $I = 520$  into the formula.

$$A = 8000 + 520 = 8520$$

The maturity value of the loan is \$8520.

The maturity value of a 3-month loan of \$4000 is \$4085. **What is the simple interest rate?**

- First find the amount of interest paid.

$$A = P + I$$

$$I = A - P = 4085 - 4000 = 85$$

- Find simple interest rate by solving  $I = Prt$  for  $r$

$$I = Prt \qquad 85 = 4000(r)\left(\frac{3}{12}\right)$$

$$85 = 1000r$$

$$0.085 = r$$

$$r = 8.5\%$$

Write the decimal as a percent.

The simple interest rate on the loan is 8.5%.

**Compound Interest:**  $A = P\left(1 + \frac{r}{n}\right)^{nt}$

- A = Amount of money accumulated, including interest.
- P = Principal: 500 800 2000 5000
- r = Annual % Rate: 6.00 8.00 12.00 15.00
- t = # of Years: 1 10 25 50
- n = Compounded (Times/Year): 1 1 1 1

Total:	530.00	1,727.14	34,000.13	5,418,287.21
Compounded (Times/Year):	12	12	12	12
Compound Interest:	530.84	1,775.71	39,576.93	8,629,569.61

Calculate the compound amount when \$10,000 is deposited in an account earning 8% interest, compounded semiannually, for 4 years.

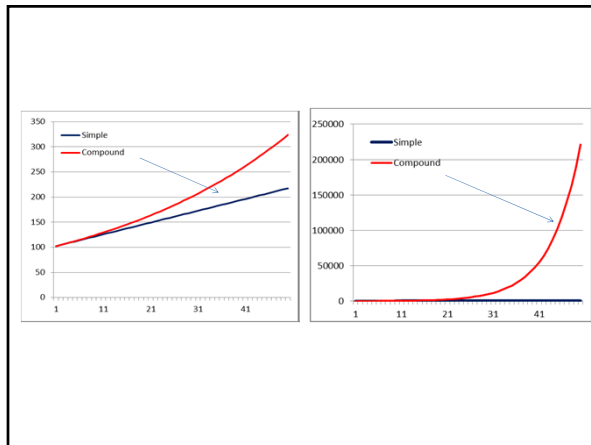
- $P = 10,000, r = 8\% = 0.08, n = 2, t = 4$

$$A = P\left(1 + \frac{r}{n}\right)^{nt} = 10,000\left(1 + \frac{0.08}{2}\right)^{2 \cdot 4}$$

$$A = 10,000(1 + 0.04)^8 = 10,000(1.04)^8$$

$$A \approx 10,000(1.368569) \approx 13,685.69$$

The compound amount after 4 years is approximately \$13,685.69.



Present value is used to determine how much money must be invested today in order for an investment to have a specific value at a future date.

**Present Value Formula**

The present value formula is

$$P = \frac{A}{\left(1 + \frac{r}{n}\right)^{nt}}$$

where  $P$  is the original principal invested,  $A$  is the compound amount,  $r$  is the annual interest rate,  $n$  is the number of compounding periods per year, and  $t$  is the number of years.

How much money should be invested in an account that earns 8% interest, compounded quarterly, in order to have \$30,000 in 5 years?

- $A = 30,000, r = 8\% = 0.08, n = 4, t = 5$

$$P = \frac{A}{\left(1 + \frac{r}{n}\right)^{nt}} = \frac{30,000}{\left(1 + \frac{0.08}{4}\right)^{4 \cdot 5}} = \frac{30,000}{1.02^{20}}$$

$$P \approx \frac{30,000}{1.485947396} \approx 20,189.14$$

\$20,189.14 should be invested in the account in order to have \$30,000 in 5 years.

Inflation - increases in costs of goods & services.

- Example: Your annual salary today = \$35,000.
- In 20 years, what salary will have the same purchasing power with a 6% inflation rate?

$$P = 35,000, r = 6\% = 0.06, t = 20. \quad A = P\left(1 + \frac{r}{n}\right)^{nt}$$

The inflation rate is an annual rate, so  $n = 1$ .

$$A = 35,000\left(1 + \frac{0.06}{1}\right)^{1 \cdot 20} = 35,000(1.06)^{20} \approx 35,000(3.20713547)$$

$$A \approx 112,249.74$$

You need to earn an annual salary of approximately \$112,249.74 in order to have the same purchasing power.

## Inflation

- The present value formula can be used to determine the effect of inflation on the future purchasing power of a given amount of money.
- Substitute the inflation rate for the interest rate in the present value formula. The compounding period is 1 year. Again we will assume a constant rate of inflation.

### Calculate the Effect of Inflation on Future Purchasing Power

Suppose you purchase an insurance policy in 2015 that will provide you with \$250,000 when you retire in 2050. Assuming an annual inflation rate of 8%, what will be the purchasing power of the \$250,000 in 2050?

Use the present value formula.

$A = 250,000$ ,  $r = 8\% = 0.08$ ,  $t = 35$ , annual rate, so  $n = 1$ .

$$P = \frac{A}{\left(1 + \frac{r}{n}\right)^{nt}} = \frac{250,000}{\left(1 + \frac{0.08}{1}\right)^{1 \cdot 35}} = \frac{250,000}{(1 + 0.08)^{35}} \approx \frac{250,000}{14.785344}$$

$$P \approx 16,908.64$$

Assuming an annual inflation rate of 8%, the purchasing power of \$250,000 will be about \$16,908.64 in 2050.

## Effective Interest Rate

- When interest is compounded, the annual rate of interest is called the **nominal rate**.
- The **effective rate** is the simple interest rate that would yield the same amount of interest after 1 year.
- When a bank advertises a “7% annual interest rate compounded daily and yielding 7.25%,” the nominal interest rate is 7% and the effective rate is 7.25%.

### Calculate the Effective Interest Rate

A credit union offers a certificate of deposit at an annual interest rate of 3%, compounded monthly. Find the effective rate. Round to the nearest hundredth of a percent.

Use the compound amount formula to find the future value of \$100 after 1 year.

$P = 100$ ,  $r = 3\% = 0.03$ ,  $n = 12$ ,  $t = 1$

$$A = P\left(1 + \frac{r}{n}\right)^{nt} = 100\left(1 + \frac{0.03}{12}\right)^{12 \cdot 1} \approx 103.04$$

$$I = A - P = 103.04 - 100 = 3.04$$

The effective interest rate is 3.04%.

## Effective Interest Rate

To compare two investments or loan agreements, we could calculate the effective annual rate of each. However, a shorter method involves comparing the compound amounts of each. Because the value of

$$\left(1 + \frac{r}{n}\right)^{nt}$$

is the compound amount of \$1, we can compare the value of

$$\left(1 + \frac{r}{n}\right)^{nt}$$

for each alternative.

## Compare Annual Yields

One bank advertises an interest rate of 5.5%, compounded quarterly, on a certificate of deposit. Another bank advertises an interest rate of 5.25%, compounded monthly. Which investment has the higher annual yield?

Calculate  $\left(1 + \frac{r}{n}\right)^{nt}$  for each investment.

$$\left(1 + \frac{r}{n}\right)^{nt} = \left(1 + \frac{0.055}{4}\right)^{4 \cdot 1} \quad \left(1 + \frac{r}{n}\right)^{nt} = \left(1 + \frac{0.0525}{12}\right)^{12 \cdot 1}$$

$$\approx 1.0561448 \quad \approx 1.0537819$$

An investment of 5.5% compounded quarterly has a higher annual yield than an investment that earns 5.25% compounded monthly.